



Article Design Implication of a Distribution Transformer in Solar Power Plants Based on Its Harmonic Profile

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Abstract: This article presents a comparative analysis for the design considerations for a solar power generation transformer. One of the main existing problems in transformer manufacturing is in the renewable energy field, specifically the solar power generation, where the transformer connected to the inverter is operated under a certain harmonic content and operating conditions. The operating conditions of the transformer connected to the inverter are particularly unknown for each solar power plant; thus, the transformer will be subject to a particular harmonic content, which is defined by the inverter of the solar power plant. First, the fundamental calculations for solar power plant transformer and the proposed methodology for the design calculation of the distribution pad-mounted three phase transformer are presented. Then, a design study case is described where a distribution transformer under analysis is modeled using finite element analysis in ANSYS Maxwell[®] software, where the transformer will be designed for a non-harmonic and harmonic content application. Lastly, the main design parameters, flux density, the core losses and the winding excitation voltage of the transformer are calculated and presented in results and discussion section.

Keywords: renewable energy; solar power generation transformer; finite element analysis; harmonics

1. Introduction

The operation conditions and grid integration of solar power generation (SPG) are very particular, similarly to other renewable energy generation systems such as wind power plants (WPP). Solar power generation using photovoltaics involves several technical specifications for its primary equipment, mainly for the selection and sizing of the power transformer connected to the inverter of the solar power plant (SPP). One main aspect of the power transformer operation in SPP is the current harmonic content caused by the inverter. The power transformer should be designed for specific operation conditions of SPP generation, specifically the harmonic frequencies generated by the inverter. Thus, this is the main interest of performing this study. As is well known, the study of harmonics in transformers is not a new topic in the field of research. Previous work has already used correction factors for transformer losses [1] as a tool to demonstrate how these are increased due to harmonic content and thus achieve a better understanding of the operation of the device under these conditions [2,3]; Yazdani-Asrami et al. [4] evaluate the effects of harmonic distortion on the performance of the transformers and other electrical elements are analyzed, as well as the effect harmonics have in various electrical elements that affect the electrical systems; Yazdani-Asrami et al. [5] studied the harmonics impacts on alternating current (AC) losses of superconductors. Sadati, S.B. et al. [6], estimated and evaluated the losses, the remained



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Copyright: © 2021 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). lifetime and loadability on the transformer considering the effects of current harmonics and ambient temperature. The impact of harmonics in transformer lifetime is important because the lifetime can be affected if the correction factors show a significant change in losses [1]. Additionally, finite element analysis software has been used to simulate the aforementioned correction factors, and to corroborate the calculation of the increase in losses and currents for a transformer [7,8], Yazdani-Asrami et al. [9] uses simulation of finite element method (FEM) to analyze non-sinusoidal voltage effects on no-load loss of transformers, such as different electromagnetic parameters such as flux lines, flux density, losses under different input sources and with high accuracy. The proposed methodology in this work will include the results of the correction factors in the manufacturer's design system, particularly in the estimation calculation of loss increase, the volts per turn for each winding, the magnetic field density, and the induction currents. If the RMS value of the load current increases due to a non-sinusoidal load with specific harmonic content, the losses increase. If the losses increase, the flux density in the magnetic core increases, so it will behave as an internal source of harmonic generation, causing a reduction in the power factor [10]. Thus, it is feasible that the design will require an oversize of the magnetic core and coil based on a "k factor" to withstand the increase in flux density and prevent premature transformer failure [11,12]. However, the purpose of this research is to show that a "k factor" is not necessary, and considering the proposed methodology, the SPP transformer design can withstand the inverter harmonic load.

The proposed methodology included in the manufacturer's design system with the use of ANSYS Maxwell[®] (specialized simulation software in finite element method) will enable evaluation of whether the dimensions and quantity of the materials proposed for the magnetic core and coils of a transformer design are affected due to specific harmonic content of an inverter of an SPP, so the manufacturer can assure the efficiency and stability of the transformer during operation in an SPP. Another important aspect is that an SPP could be connected and disconnected at least three times a day, and also a disconnection of the SPP at full load or partial load condition of the transformer could occur, so the design of an SPP transformer must accomplish the operation requirements of a specific SPP.

In a specific SPP design, the use of electrostatic shield between primary and secondary winding should also be considered to reduce the probability of an insulation failure due to voltage distortion, which can reduce the lifetime of a step-up transformer in an SPP [13]. The electrostatic shielding it is aimed to attenuate noise and transients and reduce high frequency components transferred between windings in the transformer. Therefore, the SPP transformers in comparison with standard design transformers should be designed to withstand these conditions. However, in the case for distribution transformers, there is a debate about the use of electrostatic shields and its performance, arguing that they could add unwanted capacitance causing potential resonances during transients, it has already been proven that a ground connection in the secondary winding is enough to avoid the most damaging harmonics and the use of electrostatic shield only reduces the remaining noise [14]. Said, D.M et al. [1,2] clarifies how the shielding tends to reduce capacitive values between the windings resulting in less heating, less conduction of eddy currents, and consequently, a harmonic filtering. However, it is clarified that the electrostatic shield should be considered in the design, if an analysis for a particular transformer design is performed previously, and preferably considered for those applications where the secondary winding has no ground connection.

Existing research has analyzed the impact of solar panels and its harmonic effects on transformers and distribution networks through software simulations and laboratory tests [15,16]. Queiroz, H. et al. [17] shows the impacts of distributed generation in order to reduce transformer aging in a distribution transformer. Fortes, R.R.A et al. [18] and Ayub, M. et al. [19], analyze the impact of photovoltaic (PV) inverters in distribution networks and reinforces that PV inverters' current harmonic injection should be considered for analysis. Additionally, Gray, M.K. et al. [20] evaluates the effect of rooftop solar photovoltaic penetrations and its impact in distribution transformers, and the results presented reveal that solar photovoltaic generation reduces transformer aging without significant reductions in neutral current. Thus, the main contribution of this article is to establish and validate the design methodology for SPP transformers which will work under a specific harmonic content (mostly when the third, fifth and seventh harmonics are dominant) due to operation requirements of an SPP.

2. Fundamental Calculations Required for SPP

In this section, fundamental calculations required for the transformer design of an SPP will be presented. The total losses of a transformer (P_{LL}) involve the I^2R losses (P), the winding eddy–current losses (P_{EC}), and other stray losses (P_{OSL}) [1,2]. The equation for total losses in a transformer is presented in Equation (1):

$$P_{LL} = P + P_{EC} + P_{OSL} \tag{1}$$

In Equation (2), the per-unit load loss (P_{LL-R}), under rated conditions is calculated per unit, considering the sum of the per-unit I^2R losses (1 p.u.), the per-unit winding eddy–current loss (P_{EC-R}), and the per-unit other stray loss (P_{OSL-R}).

$$P_{LL-R}(pu) = 1 + P_{EC-R}(pu) + P_{OSL-R}(pu)$$
(2)

The winding eddy–current losses under rated conditions (P_{EC-R}), are defined as a portion of the total stray loss under rated conditions (P_{TSL-R}), where 33% of the total stray loss is assumed to be winding eddy losses for liquid-filled transformers and 67% for dry-type transformers [2]. Nevertheless, it should be mentioned that in this analysis the winding eddy current losses under rated conditions (P_{EC-R}) and other stray losses (P_{OSL-R}) will be calculated with the design tool of the transformer manufacturer. In order to estimate the increase in winding eddy current stray losses and other stray losses due to non-sinusoidal load, two correction factors for each type of loss (F_{HL}) are used, which is the ratio of the total winding eddy current losses due to the harmonics (P_{EC}), to the winding eddy current losses at the power frequency, when no harmonic currents exist (P_{EC-O}), and the harmonic loss factor for other stray losses (F_{HL-STR}) [2]. The harmonic loss factor equations are presented in Equations (3) and (4):

$$F_{HL} = \frac{\sum_{h=1}^{h=h_{max}} \left[\frac{I_h}{T}\right]^2 h^2}{\sum_{h=1}^{h=h_{max}} \left[\frac{I_h}{T}\right]^2}$$
(3)

$$F_{HL-STR} = \frac{\sum_{h=1}^{h=h_{max}} \left[\frac{I_h}{T}\right]^2 h^{0.8}}{\sum_{h=1}^{h=h_{max}} \left[\frac{I_h}{T}\right]^2}$$
(4)

where I_h is the RMS current at harmonic order "*h*", h_{max} is the highest significant harmonic number, *I* is the RMS load current, and I_1 is the RMS fundamental load current. As a result of considering the harmonic loss correction factors, the per-unit total load loss in Equation (2) now becomes Equation (5):

$$P_{LL-R}(pu) = (1 + F_{HL} * P_{EC-R}(pu) + F_{HL-STR} * P_{OSL-R}(pu))$$
(5)

Consequently, the maximum current in the windings needs to be obtained, and therefore the maximum current of the winding is calculated with Equation (6). It should be mentioned that other stray losses do not exist in the windings, so $(F_{HL-STR} * P_{OSL-R}(pu))$ is not considered in Equation (6).

$$I_{max}(pu) = \sqrt{\frac{P_{LL-R}(pu)}{1 + F_{HL} * P_{EC-R}(pu)}}$$
(6)

Non-sinusoidal loads with a particular harmonic content, can provoke an increase in the magnetic flux of a transformer [7,8]; with this consideration and knowing that in the software design tool of the manufacturer the magnetic flux density (*B*) directly affects the no-load losses (P_{NLL}), as shown in Equation (7), the calculation of the P_{NLL} must be updated integrating the harmonic content in the calculation of *B*.

$$P_{NLL} = B * Manufacturer Material Factor$$
 (7)

where the *Manufacturer Material Factor* (*MMF*) is a calculation from the software design tool based on the core properties.

For the integration of the harmonic content in *B*, first, the calculation of *B* is shown in Equation (8).

$$B = \frac{V_{per-turn}}{4.44 * f * A_c} (Tesla)$$
(8)

where A_c is the cross-sectional area of the magnetic core, and $V_{per-turn}$ is the volts per turn in the winding, whether it is high voltage (HV) winding or low voltage (LV) winding [21]. Then, in order to obtain the volts per turn, the current increase in the windings due to the maximum current in pu presented in Equation (6) is considered; this current, defined as $I_{max(winding)}$, creates a minimum but measurable increase in the winding voltage which is needed to ascertain the volts per phase ($V_{per-phase}$), and consecutively the volts per turn ($V_{per-turn}$). The volts per turn directly affect B and is used as an input for the finite element modeling (FEM).

The $I_{\max(winding)}$ for both windings is also an input for the FEM simulation, and it is shown in Equation (9):

$$I_{\max(winding)} = I_{winding} * I_{max}(pu)$$
⁽⁹⁾

where $I_{winding}$ is the calculated current using the software design tool under rated conditions for each winding (high or low voltage). The volts per phase of the windings $(V_{per-phase})$ can be obtained by using Equation (10):

$$V_{per-phase} = \frac{1000 * Smax}{(Number of phases) * I_{\max(winding)}}$$
(10)

where *Smax* is the max apparent power resulting from the calculation of the maximum current in per-unit, and the *Number of phases* is three for a three-phase transformer. The volts per turn of the windings ($V_{per-turn}$) are calculated using Equation (11).

$$V_{per-turn} = \frac{V_{per-phase}}{Number of winding turns}$$
(11)

It should be mentioned that the *Number of winding turns*, from the primary and secondary winding, respectively, is obtained according to the winding dimensions calculated from the software design tool of the manufacturer.

In Figure 1, the proposed methodology for SPP transformer design for a specific harmonic profile is presented. In the spreadsheet section of Figure 1, the calculation of new variables are included in the design software tool for the SPP transformer. The proposed methodology in Figure 1 consists, in the first step, of obtaining values for core, winding and tank losses from the design tool of the manufacturer for the standard transformer design (also obtaining the efficiency, apparent power, impedance and data of interest), this without altering the default calculations of the design tool. In the second step, based on equations from Richard Marek et al. [2], the equations are adapted into the design tool formulas for the winding current and voltage values to arithmetically estimate the increase in the magnetic flux density due to the harmonic load profile, and thus obtain the increase in core losses. Consequently, changes in the winding and tank losses will be reflected, obtaining new values for efficiency, apparent power, and other data of interest. Both sets of values will serve as input data for the FEM simulations, and finally the data results



for both scenarios (with and without harmonic loading) are obtained for its comparison and analysis.

Figure 1. Proposed methodology for solar power plant (SPP) transformer design with a specific harmonic profile.

3. Study Case for SPP Transformer Design

In this section, a study case of a transformer design using the proposed methodology is presented. First, the specification data of an inverter and its maximum harmonic profile is required (see Appendix A, Table A1 and Table A3). With this information, the design software tool can be updated and a specific design for a particular application can be achieved and meet the specified operation requirements; for this particular case, the flux density should be 1.72 Tesla as the minimum design requirement, the efficiency should be above of 99%, and the percentage impedance should be $5.75 \pm 7.5\%$. In the following sections, the analysis is based on an actual standard transformer design (see Table A2), where the calculated variables for a standard design are compared with the calculated variables of a specific design which considers the inclusion of the maximum harmonic profile required according to the proposed methodology in Figure 1.

3.1. Assessment of Standard Design vs. Specific Harmonic Profile Design

3.1.1. Standard Design

The data required for the analysis are as follows, inverter data, transformer nameplate data, and transformer core magnetizing data curves. The detailed information of data required for the analysis is presented in the Appendix A.

In Table A2, the nameplate data for a standard design are presented. The standard design used for the analysis is modeled in ANSYS Maxwell[®], where the design geometries required for the software are the interior dimensions of core, coil, and steel holders and hardware, so a model can be stablished for FEM analysis. In Figure 2, the 3D model of the standard design for analysis is presented.



Figure 2. Standard design transformer 3D model for analysis: (**a**) transformer geometry using design system tool of the manufacturer; (**b**) equivalent geometry of the transformer in ANSYS Maxwell[®].

First, loss calculations of the transformer were performed in the manufacturer's design system tool, and the total losses at no load and load conditions were obtained before applying the correction factors. The calculated losses are presented in Table 1.

Table 1.	. Transformer	standard	design	calcu	lated	losses
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Losses	Watts
PPPPPPP	4088.4
P_{ECL}	635.8
Р	14,407.8
P_{OSL}	1768
Total Losses	20,900

For the calculation of specific harmonic profile transformer design, first, the standard design calculated losses are obtained in Section 3.1.1. Then, the manufacturer's design system tool is used again and the F_{HL} and F_{HL-STR} correction factors, $P_{LL-R}(pu)$ and $I_{max}(pu)$, are calculated. Additionally, the increase in the apparent power is calculated, multiplying the nominal apparent power by the calculated $I_{max}(pu)$ in order to subsequently obtain the increase in the HV winding and LV winding currents, which are the inputs required for the finite element simulation in ANSYS Maxwell[®]. The calculated apparent power and HV and LV winding currents are presented in Table 2.

Table 2. Apparent power and winding currents in the transformer design calculated under the harmonic profile.

Design Parameters	Value
Apparent Power	2781.057 kVA
High voltage (HV) winding current.	26.866 A
Low voltage (LV) winding current.	2428.53 A

With the calculated apparent power and winding currents, the $V_{per-phase}$ and $V_{per-turn}$ can be obtained using Equations (10) and (11); it should be mentioned that for this design, the number of turns of secondary winding was nine. The calculated $V_{per-turn}$ was 42.41 V, and the $V_{per-phase}$ results are presented in Table 3. By using Equation (8) and considering the $V_{per-turn}$ calculated, the flux density *B* was 1.7989 T. Next, the transformer losses including the harmonic profile were calculated and are presented in Table 4. Additionally, the transformer efficiency was calculated by using the manufacturer design software tool considering different load percentages to ensure the proper operation under different conditions. The results are presented in Table 5.

Transformer Winding	$V_{per-phase}$	
HV winding	36,211.7 V	
LV winding	381.72 V	

Table 3. Transformer winding voltages calculated under the harmonic profile.

Table 4. Transformer losses with harmonic profile design calculated.

Losses	Watts	
P_{NLL}	5135.15	
P_{ECL}	642.18	
Р	14,407.8	
P_{OSL}	1769.07	
Total Losses	21,954.2	

Table 5. Transformer efficiency with harmonic profile calculated.

Transformer Load (%)	Harmonic Profile Efficiency (%)
25	99.12
50	99.33
75	99.30
100	99.21

3.1.2. Manufacturer Design System Parameters Results

The calculation results for standard design and harmonic profile design are presented. In Figure 3, the results obtained are summarized and presented for both designs, standard and harmonic profile.



Figure 3. Percentage changes between transformer standard design and harmonic profile design.

As shown in Figure 3, the Harmonic Profile Design showed a difference in all the design parameters considered including the calculated impedance percentage, which was 4.27 for standard design and 4.17 for harmonic profile design.

In Figure 4, a percentage change in losses calculation can be observed; this percentage change for Harmonic Profile Design is adequate and meets the requirements for this particular SPP. Therefore, the minimum design requirements are fulfilled for this stage of the design.



Figure 4. Percentage changes in losses between transformer standard design and harmonic profile design.

3.1.3. FEM Analysis Using ANSYS Maxwell®

FEM analysis using the input variables from the previous section such as *Number of* winding turns, $I_{max(winding)}$ in Equation (9) and $V_{per-turn}$ in Equation (11) was performed using ANSYS Maxwell[®]. The objective was that the meshed models of the core, winding, tank, and steel holders were generated correctly, so the winding voltages, the flux density, and the core losses could be calculated by the software and a final design could be defined by comparing the results from ANSYS Maxwell[®] and the manufacturer Design System.

Finite element solvers such as ANSYS Maxwell[®] have their own methodology and formulation to converge into a result in electromagnetic problems. For this work, the formulation A-phi [22] offered by ANSYS Maxwell[®] was used as a solver in the study, which, in its mathematical formulation, converges Maxwell's equations for its solution [23].

For the meshing, based on the type of data of interest for the study, the adaptive mesh with tetrahedral elements offered by ANSYS Maxwell[®] was used, ensuring that the meshing was identical for each simulation.

3.1.4. Simulation Results for a Standard Design

The simulation was performed using, as input data, the parameters obtained from the manufacturer design system software. In Figure 5, the winding excitation voltage results from the simulation are presented, where the maximum peak value for HV winding is 33.75 kV and for LV winding is 500 V. These results are adequate, mainly because they are similar to the nominal voltages of the study case transformer in Table A2.



Figure 5. Cont.



Figure 5. Winding voltage waveforms of the standard design transformer: (**a**) HV winding; (**b**) LV winding.

In Figure 6, it can be observed the generated meshed model of the transformer under study (see Appendix A, Table A2 and Figure A1). The flux density simulation distribution in the core of the transformer had a maximum value of 1.7911 Tesla and the maximum value of flux density in the tank was 7.43 Tesla. In Figure 6a, the maximum value is observed between phase A and phase B in the upper and lower interval core section; this occurs mainly due to magnetic induction concentration in the core due to the current flow through the windings of each phase. During the continuous simulation results, it could be seen how the magnetic induction concentrates and alternates between phase A and B and then concentrates between phase B and C, which is how the transformer works during operation. In Figure 6, the images presented are considered only in a time frame, which allows us to appreciate the maximum value of magnetic flux density in the core.



Figure 6. Flux density simulations of standard design transformer: (a) core; (b) tank.

As shown in Figure 7, the total losses (Core Loss), eddy current losses, and hysteresis losses are calculated. The total losses calculation had a maximum value of 1.04 kW.



Figure 7. Core losses of standard design transformer.

3.1.5. Simulation Result for Harmonic Profile Design

In this section, the simulation was performed using the harmonic profile design data parameters obtained from the manufacturer design system software in Section 3. In Figure 8, the winding excitation voltage results from the simulation are presented, where the maximum peak value for HV winding is 36.25 kV and for LV winding is 512 V. These results are adequate because they present a similar percentage increase according to the previous calculation in the design system manufacturer's tool.

As presented in Figure 9, the flux density simulation distribution in the core of the transformer has a maximum value of 1.8614 Tesla and the maximum value of flux density in the tank is 7.8069 Tesla. In Figure 9a, the maximum value is observed between phase A and phase B in the upper and lower interval core section; this occurs during the continuous simulation results as described in Section 3.1.5, where the magnetic induction is concentrated and alternated between phases.

As shown in Figure 10, the total losses (CoreLoss), eddy current losses, and hysteresis losses are calculated. The total loss calculation had a maximum value of 1.12 kW.

The data results obtained in FEM simulation were compared between the standard design and harmonic profile design to obtain a percentage change, as shown in Figure 11. The results show a similarity with the results using the manufacturer's design software in Figures 3 and 4, where an increase in magnetic flux density and loss is noticed, mainly in the core losses. It should be noted that the increase in total losses in the FEM analysis is 4.72% (close to 5.04% when using manufacturer's design system tool calculations shown in Figure 3) and is an indication that the design will meet the required efficiency even with the harmonic profile considered.

Additionally, in Figure 11, the FEM simulation results show an increase in the percentage of flux and are similar to the value calculated by the manufacturer's design system tool in Figure 3. However, the increase in the flux density in the core, calculated in both cases, could be dangerous for the core's material type. This may be an indication that other considerations in the design such as the electrostatic shielding could be required. These results evidence the requirement of analyzing different types of core material for SPP distribution transformer design for future studies or field experiments and knowledge of how the core material behaves for a particular harmonic profile.



Figure 8. Winding voltage waveforms of harmonic profile design transformer: (a) HV winding; (b) LV winding.



Figure 9. Flux density simulation of harmonic profile design transformer: (a) core; (b) tank.



Figure 10. Core losses of harmonic profile design transformer.



Figure 11. Ansys Maxwell[®] percentage changes in main design parameters between transformer standard design and harmonic profile design.

4. Results and Discussion

The magnetic flux density in the core is the parameter that stands out in the design, and according to the calculations performed by the manufacturer's design system in Section 3, it is observed that during rated operating conditions with the harmonic profile presented the transformer design meets the material specifications, where the flux density is below the maximum flux density of the core material (see Figure A1). In Table 6, a summary of results for main design parameters for the standard design and harmonic profile design is presented.

The percentage difference results from ANSYS Maxwell[®] simulation in Figure 11 corroborate the proportionality of change in the analysis, which concludes that the harmonic profile of the inverter does not represent a major problem for the transformer efficiency during rated operating conditions. However, the proposed methodology for SPP distribution transformers, where the harmonic profile current injection of the inverter (see Table A3) is used in the analysis, could affect the volt per turn in the windings; the results indicate an

increase in the magnetic flux density above 1.72 Tesla, which is the minimum requirement for the design.

Regarding the comparison of the obtained results in this proposal with respect to other works, we find the following: in [24], the technical requirements for a step-up transformer in a photovoltaic distribution system are outlined and the design characteristics that must be considered to guarantee the correct operation of the transformer are included. However, the percentage variation in aspects such as capacity, magnetic flux, total losses, efficiency and impedance of the proposed design with respect to a conventional design is not reported. In this work, the percentage variation is considered (see Figure 11), so we cannot contrast the benefits or deficiencies of this work with the mentioned reference.

Main Final Design Parameters	Std Design Design System Tool	Std Design ANSYS Maxwell	Harmonic Profile Design Design System Tool	Harmonic Profile Design ANSYS Maxwell
B (Tesla)	1.7141	1.7911	1.798	1.8614
Total Losses (W)	20,900	24,991	21.954	26,170
ղ (%)	99.25	-	99.21	-
HV winding max voltage	34,505	34,705	36,211	36,410
LV winding max voltage	363	520	381	530
Vper-turn	40.42	40.42	42.41	42.41
$I_{max}(pu)$	1	1	1.04945	1.049

5. Conclusions

The calculations and analysis carried out in this work indicate that the harmonic profile considered in the design process (see Figure 1) concludes that the final transformer design will operate correctly at the particular operating conditions in an SPP being considered without the requirement of a "k" factor design and without any filter inside the transformer.

For a specific harmonic profile design, it is suggested to use the loss correction factors mentioned in Section 2 to estimate the increase in apparent power and loss of the transformer design, and the harmonic profile should be indicated by the user of the SPP distribution transformer.

For future work and recommendations, it is suggested to perform physical experimentation for the designs. The scope of ANSYS Maxwell[®] software can add greater value if it is correlated with laboratory tests. Additionally, it should be mentioned that, in this type of transformer, an electrostatic shield is usually considered to reduce the harmonic effect into the core and coil. With the appropriate shield design, the transformer design could be robust enough to withstand harmonic loads for SPP applications. Nevertheless, in this work the electrostatic shield was not considered in the design, and the use of an electrostatic shield could be analyzed in future work, including ANSYS Maxwell[®] simulations in order to determine the effect of the shield in the magnetic flux density.

Therefore, physical tests on transformers designed for SPP with and without electrostatic shields with a star delta connection should be performed to evaluate their performance. In the same way, an integration of the FEM simulations is recommended as an external module in the design system tool of the transformer manufacturer.

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Abbreviations

Abbreviation	Definition
B	Magnetic Flux Density
FEM	Finite Element Modeling
FIII	Correction Factor for Winding Eddy–Current Losses
FILL CTTD	Correction Factor for Other Stray Losses
HL-SIK	High Voltage
I	Current
I D	Desistance
	Levy Voltage
	Low voltage
MIMF	Manufacturer Material Factor
P	I ⁻ R Losses
P_{EC}	Winding Eddy–Current Losses
P_{EC-R}	Per-unit Winding Eddy–Current Losses
P_{EC-O}	Winding Eddy–Current Losses when no Harmonic Currents exist
P_{LL}	Total Losses of a Transformer
P_{LL-R}	Per-unit Load Losses
P_{NLL}	No Load Losses
P_{OSL}	Other Stray Losses
P_{OSL-R}	Per-unit Other Stray Losses
P_{TSL-R}	Per-unit Total Stray Losses
PV	Photovoltaic
RMS	Root Mean Square or Effective
S	Apparent Power
SPG	Solar Power Generation
SPP	Solar Power Plant
V	Voltage
W	Watts
WPP	Wind Power Plants

Appendix A

Table A1. Inverter data.

	Rated Power	2.7/2.7	MW/MVA
	AC Rated Voltage (3-Phase)	600 + 10%	V
	Rated Frequency	60/50	Hz
AC Output Side	Rated Current	2598	A RMS
AC Output Side	Power Factor	0.926	Lead/Lag
	Maximum Current	2598	ARMS
	Maximum Efficiency	98.80	%
	Rated Efficiency	98.50	%
DC Input Side	Maximum DC voltage	1500	V
DC input side	DC Voltage operation range	875-1200	V

Table A2. Distribution transformer required data.

	Distribution Transformer Data	
Operation Configuration	Step-up low voltage input and high voltage output	
Rated Voltage	34.5/0.630	kV

Table A2. Cont.

	Distribution Transformer Data	
Rated Power	2.7	MVA
Rise Temperature	65	°C
Rated Frequency	60	Hz
Impedance	4.27	%
Efficiency	99.25	%
Connection	Delta/Star-Grounded	
HV and LV Winding material	Aluminum	

 Table A3. Inverter data—harmonic profile.

Harmonic Order	Phase A (A)	Phase A (%)	Phase B (A)	Phase B (%)	Phase C (A)	Phase C (%)
1	2610.37	99,988	2572.83	99.981	2661.82	99.989
2	10.93	0.418	21.5	0.835	6.45	0.242
3	15.14	0.58	25.49	0.991	20.7	0.778
4	3.57	0.137	5.84	0.227	6.05	0.227
5	31.78	1.217	32.94	1.28	29.07	1.092
6	1.51	0.058	1.86	0.072	1.16	0.044
7	9.96	0.382	9.89	0.384	11.33	0.426
8	3.9	0.149	2.06	0.08	2.48	0.093
9	0.8	0.031	1.03	0.04	1.69	0.064
10	0.3	0.011	2.24	0.087	1.93	0.073
11	4.81	0.184	5.0	0.195	4.4	0.165
12	0.86	0.033	1.02	0.04	0.76	0.028
13	1.31	0.05	0.77	0.03	1.47	0.055
14	0.19	0.007	1.94	0.075	2.12	0.08
15	0.5	0.019	1.04	0.04	1.23	0.046
16	1.18	0.045	1.08	0.042	2.01	0.075
17	2.27	0.087	3.05	0.118	0.77	0.029
18	0.75	0.029	0.22	0.009	0.94	0.035
19	2.53	0.097	4.09	0.159	2.91	0.109
20	2.9	0.111	1.69	0.066	1.67	0.063
21	1.08	0.041	1.02	0.04	0.07	0.003
22	3.34	0.128	3.78	0.147	3.22	0.121
23	0.9	0.034	1.16	0.045	0.43	0.016
24	0.13	0.005	0.43	0.017	0.46	0.017
25	0.63	0.024	0.57	0.022	0.46	0.017
26	1.76	0.067	2.15	0.084	2.02	0.076
27	0.24	0.009	0.27	0.011	0.31	0.011
28	0.54	0.021	0.98	0.038	0.89	0.034
29	0.22	0.008	0.25	0.01	0.05	0.002
30	0.09	0.003	0.26	0.01	0.28	0.011
31	0.09	0.003	0.11	0.004	0.05	0.002
32	0.22	0.009	0.21	0.008	0.32	0.012
33	0.12	0.005	0.02	0.001	0.15	0.006
34	0.05	0.002	0.22	0.009	0.21	0.008
35	0.03	0.001	0.07	0.003	0.08	0.003
36	0.17	0.006	0.14	0.005	0.16	0.006
37	0.13	0.005	0.23	0.009	0.19	0.007
38	0.19	0.007	0.26	0.01	0.18	0.007
39	0.05	0.002	0.06	0.002	0.08	0.003
40	0.1	0.004	0.25	0.01	0.25	0.01
41	0.12	0.005	0.1	0.004	0.15	0.006
42	0.07	0.002	0.04	0.001	0.03	0.001
43	0.1	0.004	0.12	0.005	0.07	0.003
44	0.25	0.01	0.22	0.009	0.24	0.009
45	0.06	0.002	0.08	0.003	0.01	0
46	0.81	0.031	0.94	0.037	0.81	0.03
47	0.06	0.002	0.06	0.002	0.06	0.002



Figure A1. Magnetization curves of selected transformer magnetic core: (**a**) magnetization curve (hysteresis); (**b**) magnetization curve (material quantity relationship).

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